

## METHOD AND APPARATUS FOR GENERATING AN INTERLEAVED CODE

### CROSS REFERENCE TO RELATED APPLICATION

This application claims priority from U.S. Provisional Patent Applications Serial No. 60/164,944, entitled "Interleaved Code Structure," and Serial No. 60/164,945, entitled "Interleaved Code Detection" both filed November 12, 1999. The disclosure of those provisional patent applications are incorporated herein by reference in their entirety.

### BACKGROUND OF THE INVENTION

#### Field of the Invention

The present invention relates to digital data transmission systems and, more particularly, to coding structures and techniques for use in digital data transmission systems.

#### Description of the Related Art

When a transmitter sends a signal pattern that, by pre-arrangement, a receiver expects, this has the potential both to transmit timing information and provide for range measurement, namely determining the distance between the transmitter and the receiver. But the receiver's measurement of the time of arrival of the expected pattern depends both on the range and on the difference between the transmitter's and the receiver's timing, or internal clocks. Thus, the measurement is called a pseudorange. If the range were known, the time difference could be determined; or if the time error were negligible, the range could be determined. But usually there are both range and time uncertainties. In some applications, such as in the Global Positioning System (GPS) described in more detail below, multiple transmitters permit multiple pseudorange measurements; and, according to linear mathematics, when there are more knowns (e.g., measurements) than unknowns (e.g., uncertainties), the unknowns can be calculated.

In other applications, the expected pattern is simply a preamble to a message, and detecting the preamble pattern indicates the precise timing of the start of the message. In these applications, the timing and range uncertainties are not a problem because they

1 apply equally to the preamble and to the message. Start-of-message timing, or detecting  
2 the start of a message, is especially important when the message is encrypted, because the  
3 message will not be recovered correctly if the decryption process is started at the wrong  
4 time.

5 In any case, a single pulse or simple signal feature does not convey timing  
6 reliably, because noise can easily obscure such a signal. Repeating a simple pattern (such  
7 as 010101...) is more reliable, but is ambiguous because the first "01" is indistinguishable  
8 from the second and third "01", for example. Thus, the pattern generally needs to be  
9 complex.

10 A pseudorandom code (also called a pseudonoise, or PN code), such as a  
11 maximum-length binary code (m-sequence), is often used to transmit timing information,  
12 because such codes are ideal for reliably detecting the time of arrival of a signal in the  
13 presence of noise. The code can be sent repeatedly, in which case the timing is analogous  
14 to the ticking of a clock with each repetition of the code corresponding to a clock tick.  
15 This code can be combined with other data that effectively identifies each 'tick' as distinct  
16 from the others, thus providing more complete time information such as the precise time  
17 of day. When noise is present, making the detection of the signal unreliable, repeating  
18 the code provides multiple opportunities to detect the timing.

19 An example of a system that uses PN codes is the Global Positioning System  
20 (GPS). The GPS system is a satellite based navigation system in which a receiver  
21 receives signals from a constellation of satellites and determines its position in three  
22 dimensions and determines the time. A GPS receiver determines its position and the time  
23 based on ranging measurements to several satellites. The ranging measurements are  
24 made based on the propagation delay of signals transmitted by the satellite and received  
25 by the receiver. The precision of those ranging measurements depends on the receiver's  
26 ability to synchronize its clock with the satellites' clocks. Accordingly, transferring  
27 timing information is an important feature in the GPS system.

28 In order to accurately make the ranging measurement and transfer timing  
29 information the GPS satellites transmit two signals using at least two PN codes, the so-  
30 called coarse acquisition (C/A) and precision (P) codes. The C/A code is 1023 bits long  
31 and repeats every millisecond with a chip rate of 1.023 MHz. The P code is much longer  
32 and repeats once per week, and is broadcast at a chip rate of 10.23 MHz, and therefore

1 provides higher precision. Using the longer P code to make pseudorange measurements  
2 avoids ambiguities in time differences between the satellite's clock and the receiver's  
3 clock. Also, as discussed in more detail below, the longer code provides better noise  
4 tolerance than a short code.

5 Because the C/A code is short and repeats often, it is relatively easy to detect and  
6 acquire. However, because the P code is so long it is very difficult if not impossible to  
7 acquire it without at least some measure of timing information about the phase of the P  
8 code. Superimposed on the C/A code is a navigational message that provides a longer  
9 cycle of timing and related information. Once a receiver acquires the C/A code it can  
10 extract timing information from the C/A code for use in acquiring the longer P code.  
11 Accordingly, two separate signals, carrying different length codes are used in time  
12 transfer applications such as in the GPS system.

13 The use of a short code to help acquire a longer code can be illustrated with the  
14 GPS system. In acquiring a coded signal a receiver must search for a specific portion of  
15 the code to detect its phase. To start its search a receiver must "guess" at certain search  
16 parameters. For example, in the case of the C/A code, there are 1023 possible starting  
17 positions for the code; and only one guess out of 1023 is correct. Usually, this is doubled.  
18 A receiver is designed to guess at half-chip intervals – because it does not know when  
19 any chip starts. But even when a receiver determines the correct guess, it still cannot  
20 distinguish one millisecond instance of the code from another, and this is known as  
21 ambiguity. In the case of the P code, if the receiver knows the time to within one second  
22 (plus or minus a half-second), then there are 10,230,000 possible starting positions for  
23 the code; and only one guess out of 10,230,000 is correct. It will take about 10,000 times  
24 longer to search the longer P code by testing the possibilities, however, there will be no  
25 ambiguity when the search is completed. But if the receiver first acquires the C/A code  
26 timing, it can determine when millisecond periods of the code start, even though they  
27 look alike because the same pattern repeats every millisecond. Knowing the C/A code's  
28 phase reduces the possibilities for the P-code phases to 10,000. That is, acquiring the  
29 C/A code signal helps the P code signal acquisition go 1023 times faster.

30 The code can also be sent once, generally to precisely mark the beginning of a  
31 message. An analogy for this situation is a starter's pistol marking the start of a race.  
32 When the code is sent only once, there is only one opportunity to detect the timing (for

each message). For example, this is essentially the method used by the GPS cross-links (between satellites). The SINCGARS radio, a battlefield radio commonly used by the U.S. military, repeats a short code for a limited time and inverts the last repetition once before each message transmission. This last repetition corresponds to the code being sent once to mark the beginning of the message that follows the code. However, a burst of noise coinciding with this one-time code transmission will cause the system to fail and the message will be lost.

Fig. 1 shows a transmitter 1 and a receiver 9 used in a spread-spectrum system such as the GPS system. The transmitter includes a PN code generator 2 that is driven by a timing counter 3 and both are run based on a clock oscillator 4. The PN code generated by generator 2 is modulated with a carrier signal via modulator 5 which is driven by carrier oscillator 6. Optionally, data can be superimposed onto the code and carrier by using a modulo 2 adder 7. The transmitter 1 transmits the modulated carrier via antenna 8 to a receiver 9.

Receiver 9 receives the transmitted signal via an antenna 10 that provides the received signal to a demodulator 11. The demodulator 11 is driven by a carrier oscillator 12, and produces two signals out-of-phase by  $90^\circ$ . Those signals are designated as in-phase (I) and quadrature (Q) signals. These two out-of-phase signals are provided to a group of parallel correlators 13. The parallel correlators can include as many, and even more, correlators as the number of phases of the code to be tested. For example, if the code length is 1023 symbols, or chips, the parallel correlators 13 can consist of 1023 correlators, one correlator for each possible phase of the code. Multiple banks of the parallel correlators 13 can be used to correlate different signals, such as in this case where one bank correlates the I-signals and another bank correlates the Q-signals. The parallel correlators 13 are also provided with PN reference codes that correspond to the PN codes generated in the transmitter. PN code generator 14 generates the reference codes. The reference codes can be delayed to correspond to the various phases to be tested. Alternatively, the input signals, here the I and Q signals, can be delayed with various delays and correlated with a single PN code to test the different phases. The PN code generator 14 is driven by a local clock oscillator 15 and timing counters 16 which can effect the different timings for the PN reference codes. The local clock oscillator also drives timing counters 16.

The communications system shown in Fig. 1 shows the acquisition mode portion of the receiver. In the acquisition mode the receiver must resolve many concurrent uncertainties; but once these uncertainties are resolved, the receiver can enter the tracking mode which performs only comparatively minor adjustments to keep the receiver's timing locked onto the timing of the received signal. Table 1 below summarizes the uncertainties involved in acquiring a spread spectrum signal and the conventional strategies employed to resolve the uncertainties.

TABLE 1

Uncertainty	Strategy
Unsure of carrier phase	Process both I and Q phases
Unsure of carrier frequencies	Try several nearby frequencies (range depends on Doppler/frequency uncertainty)
Unsure of carrier phase	Process both I and Q phases
Unsure of clock (symbol/chip) timing	Sample at twice the symbol/chip rate (e.g., 2 timing guesses per chip)
Unsure of code phase	Try correlating at all possible code phases (range depends on time uncertainty or code period)

When attempting to acquire a spread-spectrum signal the receiver initially does not know the correct carrier phase, so the conventional strategy is to process the signal with the two carrier phases signals, the I and Q signals, because at least one of these phases will be close enough to detect the signal, if the carrier frequency is set accurately enough that the phase does not rotate more than about 90 degrees during any given correlation. Each sample has an I and a Q component, also called I and Q data.

If the frequency uncertainty is too great, typically when the transmitter and/or receiver are moving, then the receiver will try to use a sufficient number of frequencies to cover the range of uncertainty. These different frequencies are often called Doppler bins, when the Doppler effect is the largest contributor to the frequency uncertainty.

1           The receiver also initially does not know the correct clock (chip) phase, although  
2 typically it can set the clock frequency close enough to enable detection. The  
3 conventional strategy is to sample the received signal at twice the chip rate. Among the  
4 odd samples and even samples, at least one of these sample sequences will be close  
5 enough to the ideal timing to detect the signal.

6           Finally, the receiver initially does not know the timing of the PN code. For a  
7 repeated  $n$ -chip code, there are  $n$  code timing possibilities. If the repeat cycle (i.e., the  
8 code length) is shorter than the time uncertainty of the receiver, the code will not, by  
9 itself, resolve all of the receiver's time uncertainty. If the code length is greater than the  
10 range of the receiver's time uncertainty, then the number of code timing possibilities is  
equal to the number of chips in the range of the receiver's time uncertainty.

11           The receiver can find the correct carrier frequency and phase and correct chip and  
12 code timing faster to the degree that it has more correlators. The correlations of I and Q  
13 data are usually combined and counted as one correlation. When a short code such as the  
14 C/A code is repeated, it is common practice to provide enough correlators operating  
15 concurrently (i.e., "in parallel") to try all code phases, both odd and even chip samples,  
16 and to process both I and Q data. Some parallel correlator designs are based on delaying  
17 the reference code to obtain different alignments with the received data. Other designs  
18 are based on delaying the received signal samples to obtain different alignments with the  
19 reference code. In either case, each correlation spans one code length, and each  
20 correlation starts and ends at a different time. Thus, one correlation is produced per  
21 sample period. A set of correlations may need to be repeated for each Doppler bin, or  
22 frequency guess.  
23

24           However, when the code length is long, such as with the GPS P code, the number  
25 of correlations needed to detect the code phase becomes unreasonably large, and other  
26 methods must be used to detect the phase of the long code. For example, in the GPS  
27 system a separate signal is broadcast using the shorter C/A code to assist in detecting the  
28 longer P code.

29           Whether the code is repeated or transmitted only once, there are many suitable  
30 codes and code generators that are known and can be used. Generally, the code is  
31 detected in a receiver by one or more correlators that compare the noisy received signal  
32 with a noise-free reference code generated at the receiver. A conventional PN code

generator 9 is shown in detail in Figure 2. The PN code generator of Fig. 2 includes a shift register 20 and a modulo-2 adder 21. In this example, the shift register is six bits long, although it can be longer or shorter as needed. The six flip-flops of shift register 20 are synchronously driven by a clock signal. Modulo-2 adder 21 adds the first and sixth bits of the shift register, and inserts the result into the first position of register 20. In this manner, a maximal-length PN sequence is produced.

The receiver can use the same code generator as the transmitter thereby ensuring that the codes are identical. Each correlator effectively computes the sum of the products of received bits times reference bits. The output of a correlator is greatest when its received signal input and reference code input are time-aligned, or in-phase with one another, and small when not aligned, or out-of-phase with one another. Increased noise makes this correlation product increasingly unreliable.

At the outset, the correct time alignment between the received code and the reference code is unknown, so the receiver must try all possible alignments. For fast detection, a receiver typically will provide one correlator for each possible alignment, to try all alignments simultaneously. The alignments are spaced closely enough that at least one correlator will be sufficiently aligned to detect the code. The set of alignments is achieved either by delaying the reference code by successive small amounts, such as one bit at a time, or by delaying the received signal. Alternatively, a receiver can try the phase alignments sequentially, reducing the number of correlators, and thereby reducing the hardware cost but increasing the search time and thereby increasing the time cost. The simultaneous and sequential correlation methods can be combined, but the hardware cost times the time cost is proportional to the number of possible time alignments.

The outputs of the correlators are compared, and the correlator with the highest output indicates the correct alignment. Since the timing of the reference generator is known, and the delay used with the correlator that provides the strongest output is known, the timing of the signal, although obscured by noise, is then known.

It is established in theory and in practice that if the length of the code is multiplied by  $n$ , equal performance, namely reliable detection, can be obtained with  $n$  times as much noise power, for the same signal power and other factors. The longer code period also provides more timing information. But this increases, by  $n$ -fold, the number of

1 alignments that must be tried, thus also the number of correlations and the size of the  
2 correlator sums. This increases some costs  $n$ -fold, and other costs even more.

3 Alternatively, shorter codes can be used and the correlation can be summed over  
4  $n$  repetitions of the code. This also increases the size of the correlator sums, and related  
5 costs, and the longer correlation can handle  $n$  times as much noise power. But summing  
6 over repetitions of the shorter code does not provide more timing information, because  
7 the number of identifiable code alignments is not changed.

8 For example, suppose a communications system uses a code one second long that  
9 repeats. The receiver finds a maximum correlation, or detects a code alignment, once per  
10 second (like a one-second clock tick). A double-length (two second) correlation can  
11 handle twice as much noise, but there is still one alignment per second. A two-second  
12 correlation on a two-second code will also handle twice the noise, but will have one  
13 alignment every two seconds. The receiver acquires more timing information with the  
14 two-second code, because it can distinguish odd and even seconds. But the longer code  
15 has twice as many possible phase positions, which doubles the cost.

16 Accordingly, conventional data transmission systems that use long PN codes have  
17 used expensive hardware solutions or employ two separate signals with different codes,  
18 with the associated hardware costs and complexities, such as in the GPS system discussed  
19 above, to acquire and use the more noise tolerant long codes in a timely manner.

## 20 21 SUMMARY OF THE INVENTION

22 Therefore, in light of the above, and for other reasons that will become apparent  
23 when the invention is fully described, an object of the present invention is to provide a  
24 relatively long code by interleaving two shorter codes.

25 A further object of the present invention is to generate a code with good noise  
26 tolerance that can be detected quickly with a relatively low hardware cost.

27 Yet a further object of the present invention is to provide a signal with increased  
28 noise tolerance.

29 A still further object of the present invention is to provide a signal that can be  
30 effectively received in the presence of a jamming signal.

31 Another object of the present invention is to provide a pseudonoise code signal  
32 by interleaving two shorter pseudonoise noise signals.



1           The aforesaid objects are achieved individually and in combination, and it is not  
2 intended that the present invention be construed as requiring two or more of the objects  
3 to be combined unless expressly required by the claims attached hereto.

4           In accordance with one aspect of the invention, there is described a code  
5 generating apparatus, including a first code generator generating a first code of  $n$   
6 symbols; a second code generator generating a second code of  $m$  symbols, where  $m$  is  
7 greater than  $n$ ; and a combiner for combining the symbols generated by the first and  
8 second code generators to generate a combined code for which both the first and second  
9 codes can be detected. The combiner can be a multiplexer that interleaves the symbols  
10 of the first and second codes to generate an interleaved code. Also,  $n$  and  $m$  preferably  
11 are mutually prime, and can be such that  $m=n+1$ , and the first and second codes can be  
12 pseudonoise (PN) codes.

13           In accordance with another aspect of the invention, there is described a method  
14 of generating a combined code including, combining a plurality of codes each having a  
15 length shorter than the transmission code, and outputting the combined code. The  
16 plurality of codes can be detected from the combined code, and the phase of the  
17 combined code can be detected from the plurality of codes.

18           In accordance with yet another aspect of the invention, there is described a  
19 method of generating a code, including generating a symbol of a first code of length  $n$   
20 symbols; generating a symbol of a second code of length  $m$  symbols, where  $m$  is greater  
21 than  $n$ ; and generating a third code by outputting the symbol of the first code followed  
22 by the symbol of the second code. The first and second codes can be PN codes, and  $m$   
23 and  $n$  preferably are mutually prime and can be such that  $m=n+1$ .

24           In accordance with still another aspect of the invention, there is described a  
25 transmitter, including a controller outputting first, second and third control signals based  
26 on a count; a first code generator generating a first code of  $n$  symbols in response to the  
27 first control signal; a second code generator generating a second code of  $m$  symbols in  
28 response to the second control signal; and a combiner coupled to the controller and the  
29 first and second code generators, wherein the combiner in response to the third control  
30 signal combines the symbols of the first code with the symbols of the second code and  
31 outputs a combined code. The combiner can be a multiplexer that interleaves symbols  
32 of the first code with symbols of the second code, thereby outputting the combined code

1 as an interleaved code. Also, the first and second codes can be PN codes, and m and n  
2 preferably are mutually prime and can be such that  $m=n+1$ .

3 In accordance with still yet another aspect of the invention, there is described a  
4 transmission signal having a sequence of symbols, the sequence including symbols of a  
5 first code of n symbols interleaved with symbols of a second code of m symbols. The  
6 first and second codes can be PN codes, and m and n preferably are mutually prime and  
7 can be such that  $m=n+1$ . Also, the first code can repeat modulo n and the second code  
8 can repeat modulo m, and the sequence can repeat modulo  $2 \cdot n \cdot m$ .

9 The above and still further objects, features and advantages of the present  
10 invention will become apparent upon consideration of the following descriptions and  
11 descriptive figures of specific embodiments thereof wherein like reference numerals in  
12 the various figures are utilized to designate like components. While these descriptions  
13 go into specific details of the invention, it should be understood that variations may and  
14 do exist and would be apparent to those skilled in the art based on the descriptions herein.  
15

#### 16 BRIEF DESCRIPTION OF THE DRAWINGS

17 Fig. 1 is a block diagram of a conventional spread spectrum communication  
18 system.

19 Fig. 2 is a block diagram of a conventional pseudonoise (PN) generator.

20 Fig. 3A shows an example of two short codes to be interleaved together to form  
21 an interleaved code.

22 Fig. 3B shows the interleaved code formed from the two short codes shown in  
23 Fig. 3A.

24 Fig. 4A shows the values of the interleaved codes shown in Fig. 3A.

25 Fig. 4B shows the sequence of values of the interleaved code formed from the  
26 values of the two short codes shown in Fig. 4A.

27 Fig. 5 is a block diagram of a portion of a transmitter that generates the  
28 interleaved code.

29 Fig. 6 is a flowchart illustrating a method for generating the interleaved code.

30 Fig. 7A shows the first part of two interleaved codes to be truncated.

31 Fig. 7B shows the middle part of the two interleaved codes of Fig. 7A, that is used  
32 as the code to be transmitted and detected.

1 Fig. 7C shows the last part of the two interleaved codes of Fig. 7A, that is to be  
2 truncated.

3 Fig. 8 is a block diagram of portion of a transmitter that generates a truncated  
4 interleaved code.

### 5 6 DESCRIPTION OF THE PREFERRED EMBODIMENTS

7 The following detailed explanations of the preferred embodiments describe the  
8 best known ways of practicing the present invention.

9 The invention herein described combines two or more short codes to achieve the  
10 performance of a much longer code. For example, two codes of about one thousand bits  
11 each transmitted in about one millisecond can be combined to make a composite code of  
12 about two million bits transmitted in about two seconds. This provides one code  
13 alignment every two seconds, and increases the noise tolerance two-thousand-fold over  
14 the short code, which may be necessary if a jamming signal is present on the  
15 communication links. Although the descriptions and examples provided here will favor  
16 the case where the code is repeated, the invention also can be applied to the situation  
17 where the code is transmitted only once.

18 Summing correlations of a received signal with a 1000-bit reference code over  
19 two thousand repetitions of the 1000-bit PN code will provide the same noise tolerance  
20 as with the two million bit code, but only provides one code alignment per millisecond.  
21 Simply increasing the code length two-thousand-fold also provides the same noise  
22 tolerance, and provides one code alignment every two seconds, but would increase the  
23 cost enormously, because there are two million possible time alignments. However,  
24 using the present invention, there are two thousand possible time alignments for each  
25 code (four thousand altogether), so the combined hardware cost and time cost is reduced  
26 five-hundred-fold.

27 Sometimes two signals are used as in the GPS system. The receiver detects a  
28 short code (the first signal), then uses the partial timing information thus acquired to  
29 detect a very long code (the second signal). The processing of two signals basically  
30 doubles the cost because of more parts for the receiver, and because it involves a two-step  
31 process that presents more opportunities to fail. The present invention uses one signal,  
32 and thus effects only the cost of the code detection part of the receiver.

1 Described next is a method of constructing a long pseudonoise code from two  
2 shorter pseudonoise codes, useful for conveying time or pseudorange information over  
3 a noisy communication channel. In such applications, the pseudonoise code symbols are  
4 comprised of 'chips', and they are alternatively referred to here as "bits". Although a  
5 "chip" can be a binary digit, i.e., a "bit", the invention is not limited to use only with  
6 binary symbols.

7 In a simple case of an interleaved code according to the present invention, any  
8 relatively short code, preferably with good autocorrelation properties, is combined with  
9 another short code. That other short code can be generated by adding or deleting one bit,  
10 such as at the end of the first code. This results in deriving two short codes, one  $n$  bits  
11 long and the other  $n+1$  bits long. These two codes are then combined, such as by  
12 interleaving them, and the resulting pattern repeats after every  $2 \cdot n \cdot (n+1)$  bits. This is  
13 because  $n$  and  $n+1$  are always mutually prime. That is, the short codes do not have a  
14 common factor. Thus, a longer code of  $2 \cdot n \cdot (n+1)$  bits is generated by interleaving the two  
15 shorter codes. The invention is not limited to using codes that are mutually prime.  
16 However, if mutually prime length codes are used an interleaved code of maximal length  
17 will result.

18 More generally, two relatively short codes of lengths  $m$  and  $n$  can be interleaved,  
19 where  $m$  and  $n$  are mutually prime, thus generating a longer code of  $2 \cdot m \cdot n$  bits. More  
20 than two codes, preferably of mutually prime lengths, can be interleaved according to the  
21 invention, however using only two codes will generally minimize the cost and will suffice  
22 for many applications. Although the minimum number of short codes to be combined  
23 according to the invention is two, and hence is the simplest choice, more generally more  
24 than two codes can be combined according to the invention. For example, three or more  
25 short codes can be interleaved, or more generally, combined. Three short codes having  
26 mutually prime lengths of  $m$ ,  $n$ , and  $p$  would yield a long code of length  $3 \cdot m \cdot n \cdot p$ .

27 In general, the present invention independently detects the phase of each short  
28 code and allows the well-known Chinese Remainder Theorem to be used to derive the  
29 phase of the long code. In the simplest case, a short code A ( $n$  bits long) with bits  
30 numbered from 0 to  $n-1$ , and a short code B ( $n+1$  bits long) with bits numbered from 0  
31 to  $n$  are interleaved bit by bit or symbol by symbol to form a longer code. If the long  
32 code begins with bits A0 and B0 in the first pair of bits (pair 0), and if a receiver detects

1 bit a of code A and bit b of code B in the same bit pair, then the receiver calculates that  
2 the position of that bit pair in the long code is equal to  $(n+1) \cdot a - n \cdot b$ , adding  $n \cdot (n+1)$  if  
3 this is negative.

4 The cost of detecting short code A is proportional to the number of possible  
5 phases,  $2 \cdot n$ . The factor of two is included because the receiver initially does not know  
6 which bits are of code A, and which are of code B. Likewise, the cost of detecting short  
7 code B is proportional to  $2 \cdot (n+1)$ , so the total cost of detecting short codes A and B  
8 interleaved with one another is proportional to  $4 \cdot n + 2$ . This is much less than the cost of  
9 detecting the long code as a whole, which is proportional to  $2 \cdot n \cdot (n+1)$ . For example, if  
10  $n=1000$ ,  $4 \cdot n + 2 = 4002$  and  $2 \cdot n \cdot (n+1) = 2,002,000$ . Thus, the cost of detecting the  
11 interleaved short codes, in this example, is about 500 times less expensive than detecting  
12 the longer non-interleaved code.

### 13 *A Small Code Example*

14 Figures 3A and 3B illustrate how an interleaved code can be constructed with 5-  
15 bit and 6-bit codes according to the invention. These figures do not show the actual value  
16 of the bits but instead show the bit positions within the short codes. Here, the bits of the  
17 5-bit code (A) are named 0 1 2 3 4, and the bits of the 6-bit code (B) are named 0 1 2 3  
18 4 5. Figure 3A shows these numerical names, with the bits of code A raised slightly to  
19 make the construction easier to see. Figure 3B shows the bits of codes A and B  
20 interleaved and in sequence.

21 For the first repetition of the component codes, bit n of code B precedes bit n of  
22 code A. For the next repetition, bit n of code B follows bit n of code A. Code B, which  
23 is longer, and which therefore repeats more slowly, progressively lags behind code A  
24 until the two component codes are again nearly aligned. The composite interleaved code  
25 repeats every  $2 \cdot 5 \cdot 6 = 60$  bits, wherein the 5-bit code is repeated 6 times and the 6-bit  
26 code is repeated 5 times, for 30 bits each.

27 Figure 4A illustrates the same interleaving again, but shows the bit values. Here,  
28 the bit sequence is 00101 for the 5-bit code A, and the last bit is repeated in code B to  
29 obtain the 6-bit code 001011. Figure 4B shows the bit values of the interleaved codes in  
30 sequence, and shows how the bits are doubled in the intervals where the two component  
31 codes are nearly aligned.

1 Near the middle of the sequence shown in Figure 4A is the bit-pair  $b=5$ ,  $a=2$ .  
2 Applying the formula  $6 \cdot a - 5 \cdot b$ , results in  $-13$ , and since this is negative,  $5 \cdot 6$  is added to  
3 obtain 17, the position of the bit-pair, where the first position is 0.

#### 4 *A Larger Code Example*

5 In a practical application, the codes are likely to be much longer than the small  
6 example described above. For example, a 1023-bit maximum-length code (m-sequence)  
7 might be chosen as code A; and code B could be 1024 bits long, identical to code A, but  
8 with one additional bit at the end. This produces a composite code that is  $2 \cdot 1023 \cdot 1024$   
9  $= 2,095,104$  bits long. In an actual application, the bit rate might be 10.23 million bits  
10 per second, so that the code length is 0.2048 seconds. The entire code need not be used,  
11 and it may be convenient to use a length of exactly 0.2 seconds to more easily relate to  
12 ordinary clock time. Accordingly, the code may be truncated to exactly 2,046,000 bits,  
13 which at 10.23 MHz corresponds to a code period of 0.2 seconds. This provides an  
14 opportunity to avoid using the 2047 bits where the two component codes are nearly  
15 aligned. The arithmetic is easily adjusted to account for the number of truncated bits.

#### 16 *Transmitter*

17 The interleaved code of the invention typically would be used in a digital data  
18 transmission system having a transmitter and a receiver. The transmitter would generate  
19 the interleaved code and send it, generally with other data superimposed on it, to a  
20 receiver. The receiver would also generate the same interleaved code as a reference code  
21 in order to synchronize with the transmitter, and could then extract the data superimposed  
22 on the transmittal signal.

23 Figure 5 shows an example of a transmitter 50 that generates an interleaved code,  
24 and includes two code generators, code generator A (51) and code generator B (52). Each  
25 code generator can be a pseudonoise (PN) generator, with a structure similar to the PN  
26 generator shown in Fig. 2. The two code generators are not identical, because they must  
27 output codes of different length. Here, PN code generator A (51) outputs a PN code of  
28 length  $n$ , and PN code generator B (52) outputs a PN code of length  $m$ . Preferably,  $n$  and  
29  $m$  are mutually prime, such as when  $m=n+1$ .

30 The two outputs of the PN generators 51 and 52 are interleaved with one another.  
31 Here, a multiplexer 53 acts as a combiner to interleave the symbols, or chips, of the

1 outputs of the two code generators. Other devices that serve to combine those bits can  
2 be used. Multiplexer 53 outputs the interleaved codes to a transmission section of the  
3 transmitter (not shown) for transmission to a receiver(s). The code generators 51 and 52  
4 are controlled by a counter/controller 54 that is driven by a clock 55, so that when the  
5 code generators 51 and 52 reach the end of their codes, they are reset and begin again.  
6 The counter/controller 54 also sends control signals to multiplexer 53 to inform it when  
7 to output a symbol, or chip, from code generator A and when to output a symbol, or chip,  
8 from code generator B.

9 The interleaved code can be generated according to the following process, shown  
10 in the flowchart of Fig. 6. The process is started, as shown in Fig. 6, at operation 60, and  
11 the code generators A and B are initialized in operation 61. The clock 55 outputs a clock  
12 signal to drive counter/controller 54. The transmitter is clock driven so that if no clock  
13 signal is present the components wait, as indicated in operations 62 and 63. If a clock  
14 signal is present, as indicated in operation 62, the counter/controller 54, in operation 64,  
15 sends a signal to each of the code generators to generate the next chips in the respective  
16 code sequences. In response to the signal from counter/controller 54 each code generator  
17 modulo increments according to its code length. For example, if the length of the code  
18 generated by code generator A (51) is  $n$ , code generator A increments modulo  $n$ .  
19 Similarly, if the length of the code generated by code generator B (52) is  $m$ , code  
20 generator B increments modulo  $m$ . Each code generator outputs the generated chip to  
21 multiplexer 53, which, in operation 65, interleaves the chips into a single interleaved code  
22 that is output to a transmission section of the transmitter in operation 66.

23 For example, if code generator A outputs the sequence "1001" and code generator  
24 B outputs the sequence "10011" in successive clock cycles, the multiplexer interleaves  
25 those chips and outputs the sequence "110000111" to the transmission section. The  
26 multiplexer can interleave the codes by delaying one of the codes by one chip. This delay  
27 can occur in either the multiplexer or at the code generator. Operations 62 through 66  
28 repeat to generate and output the interleaved code.

29 As discussed above, there are instances where it may be advantageous for the  
30 interleaved code to have a period shorter than the entire period of the combined short  
31 codes. For example, it may be convenient for the interleaved code length to have a length  
32 corresponding to exactly 0.2 seconds to more easily relate to ordinary clock time.

1 Accordingly, the code may be adjusted to output exactly 2,046,000 bits at a rate of 10.23  
2 MHz. Here, in operation 61 of Fig. 6 one of the code generators could be initialized to  
3 a non-zero value so the interleaved code would begin at a later phase in the code than if  
4 it were initialized to zero. When the code generator reaches the end of its code the  
5 transmitter could reinitialize it to the predetermined initialization value, instead of to  
6 zero. This method would essentially remove bits from the front of the code. Similarly,  
7 bits can be truncated from the end of the interleaved code.

8 Figures 7A - 7C show how portions of the two short codes can be selected to  
9 achieve a truncated code with a convenient code length. Here, Fig. 7A shows a beginning  
10 portion of a combined 1023 and 1024 code. In this instance the first twelve repetitions  
11 of the 1023 length code are truncated. Accordingly, the part of the code labeled as 1023  
12 x 12 is not transmitted by the transmitter. Fig. 7B shows the middle portion of the  
13 interleaved short codes and the following twelve bits of the 1024 code selected for  
14 transmission in this example. Here, one thousand repetitions of the 1023 code along with  
15 nine hundred ninety-nine repetitions of the 1024 length code are selected for transmission  
16 by the transmitter. Additionally, twelve bits or chips of the 1024 code that are interleaved  
17 with the first twelve bits of the 1023 code that are transmitted are included, as are twelve  
18 bits of the 1024 code interleaved with the last twelve bits of the 1023 code that are  
19 transmitted. Fig. 7C shows the end portion of the interleaved code that is truncated in  
20 this example. Here, the last twelve repetitions of the 1023 code are not transmitted.  
21 Accordingly, the total number of bits transmitted in the truncated code is  $(1023 \times 1000)$   
22  $+ (1024 \times 999) + 24 \text{ bits} = 2,046,000 \text{ bits}$ , which at a rate of 10.23 MHz has a code period  
23 of exactly 0.2 seconds.

24 In another aspect of the invention depicted in Fig. 8, the counter/controller 80 is  
25 modified to include a control signal for controlling a multiplexer 81 to truncate the  
26 interleaved code as shown in Figs. 7A - 7C. The counter controller 80 controls the  
27 multiplexer 81 to interleave codes A and B so that only the symbols or chips of codes A  
28 and B corresponding to the selected symbols shown in Fig. 7B are interleaved and  
29 transmitted.

30 Other techniques for truncating or selecting only a portion of the combined short  
31 codes can be used to achieve a convenient long code length. For example, only bits at



1 either the beginning or the end of the combined sequence can be truncated to form a  
2 convenient long code length.

3 The counter controller 80, the code generators A (51) and B (52), and multiplexer  
4 81 can be implemented in hardware, software or firmware using well-known techniques.

5 Although the invention has been described in terms of two binary codes of length  
6  $n$  and  $n+1$ , other variations fall within its scope. For example, more than two codes can  
7 be interleaved to achieve the benefits of the invention. Also, two codes that are mutually  
8 prime, other than of lengths  $n$  and  $n+1$  can be used. Further, codes that are not mutually  
9 prime can be used, although the increased noise tolerance achieved with longer codes  
10 may not be realized to the maximum extent because the code would have a shorter than  
11 maximum period due to a common factor between the code lengths. While it is expected  
12 that binary codes will be used most often, the invention can be applied in systems with  
13 more than two transmission symbols.

14 Having described preferred embodiments of an interleaved code structure,  
15 techniques and devices for generating those code structures, and techniques and devices  
16 for transmitting those codes, it is believed that other modifications, variations and  
17 changes will be suggested to those skilled in the art in view of the teachings set forth  
18 herein. It is therefore to be understood that all such variations, modifications and changes  
19 are believed to fall within the scope of the present invention as defined by the appended  
20 claims. Although specific terms are employed herein, they are used in their ordinary and  
21 accustomed manner only, unless expressly defined differently herein, and not for  
22 purposes of limitation.